A cost-effectiveness differential game model to assess climate agreements *

O. Bahn[†] A. Haurie [‡]

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Abstract

In this paper, we propose a differential game model with coupled constraint to represent the possible effects of climate agreements between industrialized, emerging and developing countries. Each group of countries is represented by an economic growth model where two different types of economies, called respectively 'low-carbon' and 'carbon' can co-exist, each of which having different productivities of capital and of emissions due to energy use. We assume that each group of countries participating in the negotiations has identified a damage function, which determines a loss of GDP due to warming and has also a possibility to invest in a capital permitting adaptation to climate changes. The climate agreements we consider have two main components: (i) they define a global emission budget for a commitment period and impose it as a limit on cumulative emissions during that period; (ii) they distribute this global budget among the different coalitions of countries taking part in the agreement. This implies that the game has now a coupled constraint for all participants in the negotiations. The outcome of the agreement is therefore obtained as a generalized or 'Rosen' equilibrium which can be selected among a whole manifold of such solutions. We show that the distribution of the total budget among the different parties is a way to explore the manifold of normalized equilibria and we propose an equity criterion to determine a fair division of this total emission budget.

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[†]Associate Professor, GERAD and Department of Management Science, HEC Montréal, Montréal, Canada

[‡]ORDECSYS, Geneva, Switzerland. Honorary Professor, University of Geneva, Switzerland and Adjunct Professor, GERAD and Department of Management Science, HEC Montréal, Montréal, Canada

1 Introduction

In this paper, we model the outcome of an international agreement on climate change as an equilibrium in an open-loop dynamic game with a coupled constraint on cumulative emissions over a specific negotiated commitment period. Our objective is to analyze the global climate change issue as a competition among different growing economies, which are linked by the damage caused by climate changes due to atmospheric accumulation of their GHG emissions. The model emphasizes also the role played by adaptation in the design of optimal response by competing groups of countries to climate change. The numerical simulations presented here consider climate change as a very long-term issue for which a cost-benefit approach based on the use of damage functions by the negotiating countries lead to equilibrium solutions with delayed action to reduce emissions, a not very attractive policy from an ecological point of view. However if we use a cost-effectiveness approach, by imposing a constraint in the form of a global emission budget over the negotiated commitment period that will be compatible with maintaining temperature increase below 2°C, immediate transition toward a low-carbon economy is favored.

We represent three main regions in the World, corresponding grossly to industrialized (OECD), emerging (BRIC) and developing or rest of the world (ROW) countries, and we associate an economic growth model à la Ramsey (1928) coupled with a climate module as in Nordhaus & Boyer (2000), with a dual economy ('carbon' vs. 'low-carbon') as in Bahn & Haurie (2008) and with an adaptation capital permitting each region to partially alleviate damages caused by the temperature increase as in Bahn *et al.* (2012). We neglect the trade effects and we consider only the interdependence caused by the influence of each group of countries on the global climate change and therefore on the damage caused to the three groups. We introduce a differential game formulation of this interdependence, using the open-loop information structure. We consider that an open-loop information structure is relevant since the climate negotiations can be viewed as the search for an optimal trade-off between different and possibly conflicting economic growth paths. Several integrated models have been proposed permitting a search for an equilibrium under an open-loop information structure, in particular RICE (Nordhaus & Yang, 1996), WITCH (Bosetti *et al.*, 2007), REMIND-R (Leimbach & *al.*, 2010) and CWS (Eyckmans & Tulkens, 2006). The originality of the approach in our paper lies in the interpretation of an international agreement on climate as the introduction of a coupled constraint in a differential game. Such games have been initially proposed in

Haurie (1995) and Haurie & Zaccour (1995) and further studied in Carlson & Haurie (2000). This concept has also been used for an environmental model in Krawczyk (2005). The effect or impact of the agreement must then be evaluated as the outcome of a normalized equilibrium as defined in Rosen (1965). It is well known that a game with coupled constraint admits a manifold of normalized equilibria. In the particular situation of this climate model it can be shown (Bahn & Haurie, 2008) that each normalized equilibrium corresponds to a particular sharing of the global budget among the players (groups of countries). Therefore, an agreement would consist in allocating a specific emission budget for the commitment period to each player and letting them play a Nash equilibrium (Nash, 1950) under these decoupled constraints. The particular sharing of the global budget could be done in order to attain some fairness objective. This interpretation of climate negotiations and agreements has been exploited recently to design meta-games based on statistical emulation of a general equilibrium model (Haurie *et al.*, 2013; Babonneau *et al.*, 2013). These models captured well the macroeconomic effects, including the modifications in the terms of trade, for several coalitions of countries (7 or 11). However the issue of long-term economic growth was not tackled in these models. The present study, based on infinite horizon differential game models is focused on the analysis of these long-term effects.

The climate change issue is a very long-term concern, so we model economic growth on a very long time interval, which can be taken as infinite (∞). However the negotiations on climate are concerned essentially with the emission situation on shorter commitment periods (e.g., 2010-2050). So we represent an international agreement on climate as the introduction of a constraint on cumulative emissions over a given commitment period, corresponding to the definition of a global emission budget, and the distribution of this budget among the three groups of countries, considered now as three players. This introduces a cost-effectiveness structure in the differential game.

We compare the different outcomes corresponding in particular to the following situations:

1. BAU, a counterfactual baseline where no damage is caused by temperature increase;

2. Pareto, where a weighted sum of the welfares is maximized;

3. Nash, where the three players define growth paths corresponding to a Nash equilibrium;

4. Rosen, where the three players define growth paths corresponding to a Nash equilibrium with a coupled constraint, as indicated above.

The paper is organized as follows: in Section 2, we give a brief description of the integrated model we use. In Section 3, we define the differential game with coupled constraint and we show how the manifold of normalized equilibria corresponds to a family of Nash equilibria with specific sharing of the budget constraint. In Section 4, we present the result of a set of numerical simulations corresponding to the different equilibrium solutions discussed. And finally, in Section 5, we conclude with a discussion of the policy implications of these simulations.

2 The integrated economic growth models

This section extends the one-region Ada-BaHaMa model proposed in Bahn *et al.* (2012) to a version where the world is comprised of m independent regions. We use a continuous time formulation.

2.1 Variables

The model uses the following variables, where $j = 1, \dots, m$ is the index of each of the n regions and t the model running time:

AD(j,t)**:** reduction of damages due to adaptation measures in region j at time t, in %;

$C(j,t) \geq 0$**:** total consumption in region j at time t, in trillions (10^{12}) of dollars;

$c(j,t) \geq 0$ **:** per capita consumption in region j at time t, $c(j,t) = \frac{C(j,t)}{L(j,t)}$;

$E_1(j,t) \geq 0$**:** yearly emissions of GHG (in Gt–10^9 tons–carbon equivalent) in the carbon economy of region j at time t;

$E_2(j,t) \geq 0$**:** yearly emissions of GHG in the low-carbon economy of region j at time t, in GtC;

ELF(j,t)**:** economic loss factor in region j due to climate changes at time t, in %;

$I_i(j,t) \geq 0$**:** investment in capital K_i ($i = 1,2,3$) in region j at time t, in trillions of dollars;

$K_1(j,t) \geq 0$: physical stock of productive capital in the carbon economy of region j at time t, in trillions of dollars;

$K_2(j,t) \geq 0$: physical stock of productive capital in the low-carbon economy of region j at time t, in trillions of dollars;

$K_3(j,t) \geq 0$: physical stock of adaptation capital in region j at time t, in trillions of dollars;

$K_{3\max}(j,t) \geq 0$: maximal stock of adaptation capital in region j at time t, in trillions of dollars;

$L_1(j,t) \geq 0$: part of the (exogenously defined) labor force $L(j,t)$ of region j allocated at time t to the carbon economy, in millions (10^6) of persons;

$L_2(j,t) \geq 0$: part of the labor force of region j allocated at time t to the low-carbon economy, in millions of persons;

$M(t) \geq 0$: atmospheric concentration of GHG at time t, in GtC equivalent;

WRG(j): discounted welfare of region j;

$Y(j,t) \geq 0$: economic output of region j at time t, in trillions of dollars.

2.2 Economic modeling

In each region $j = 1, \ldots, m$, a social planner is assumed to maximize social welfare (WRG), given by the integral over the model horizon (T) of a discounted utility from per capita consumption (c) with a pure time preference discount ρ:

$$\mathrm{WRG}(j) = \int_0^T e^{-\rho t}\, L(j,t) \log[c(j,t)]\, dt. \tag{1}$$

Total labor (L) is divided between labor allocated to the carbon economy (L_1) and labor allocated to the low-carbon economy (L_2):

$$L(j,t) = L_1(j,t) + L_2(j,t). \tag{2}$$

Consumption comes from an optimized share of production (Y), the remaining being used to invest in the production capitals (carbon-intensive—K_1—and/or low-carbon—K_2), in the adaptation capital (K_3) and to pay for energy costs (energy being measured through emission levels E_i). The presence of damages (defined by the ELF factor) reduces the available production such that:

$$\begin{aligned} C(j,t) = \mathrm{ELF}(j,t)\,Y(j,t) - I_1(j,t) - I_2(j,t) - I_3(j,t) \\ - p_{E_1}(j,t)\,\phi_1(j,t)\,E_1(j,t) - p_{E_2}(j,t)\,\phi_2(j,t)\,E_2(j,t), \end{aligned} \quad (3)$$

where p_{E_i} are energy prices and ϕ_i energy conversion factors for emissions E_i. Capital stock evolves according to the choice of investment (I_i) and a depreciation rate δ_{K_i} through a standard relationship:

$$\dot{K}_i(j,t) = I_i(j,t) - \delta_{K_i} K_i(j,t) \quad i = 1, 2, 3. \quad (4)$$

Economic output (Y) occurs in the two economies according to an extended Cobb-Douglas production function in three inputs, capital (K), labor (L) and energy (measured through emission levels E):

$$\begin{aligned} Y(j,t) &= A_1(j,t)\,K_1(j,t)^{\alpha_1(j)}\,(\phi_1(j,t)\,E_1(j,t))^{\theta_1(j,t)}\,L_1(j,t)^{1-\alpha_1(j)-\theta_1(j,t)} \\ &+ A_2(j,t)\,K_2(j,t)^{\alpha_2(j)}\,(\phi_2(j,t)\,E_2(j,t))^{\theta_2(j,t)}\,L_2(j,t)^{1-\alpha_2(j)-\theta_2(j,t)} \end{aligned} \quad (5)$$

where A_i is the total factor productivity in the carbon (resp. low-carbon) economy (when $i = 1$, resp. $i = 2$), α_i the elasticity of output with respect to capital K_i and θ_i the elasticity of output with respect to emissions E_i.

2.3 Damages and adaptation

Climate change dynamics are from the DICE model (Nordhaus, 2008). First, stocks of GHGs accumulates in three reservoirs, an atmospheric reservoir (M_{AT}), a quickly mixing reservoir in the upper oceans and the biosphere (M_{UP}), and a slowly mixing deep-ocean reservoir (M_{LO}) which acts as a long-term sink:

$$\dot{M}_{AT}(t) = \sum_{j=1}^{n} (E_1(j,t) + E_2(j,t)) + \psi_{11} M_{AT}(t) + \psi_{21} M_{UP}(t) \quad (6)$$

$$\dot{M}_{UP}(t) = \psi_{12} M_{AT}(t) + \psi_{22} M_{UP}(t) + \psi_{32} M_{LO}(t) \quad (7)$$

$$\dot{M}_{LO}(t) = \psi_{23} M_{UP}(t) + \psi_{33} M_{LO}(t), \quad (8)$$

where $\psi_{i,j}$ are calibration parameters. Second, accumulation of GHGs increases the earth radiative forcing F:

$$F(t) = \eta log_2 \left(\frac{M_{AT}(t)}{M_{AT}(1750)} \right) + F_{EX}(t), \quad (9)$$

where F_{EX} is an exogenous radiative forcing term. And third, a stronger radiative forcing yields an increase in the earth's mean surface temperature T_{AT} and more gradually in the mean (deep) ocean temperature (T_{LO}):

$$\begin{aligned} \dot{T}_{AT}(t) &= T_{AT}(t) + \xi_1 \left[F(t+1) - \xi_2 T_{AT}(t) - \xi_3 \left(T_{AT}(t) - T_{LO}(t)\right)\right] \\ \dot{T}_{LO}(t+1) &= T_{LO}(t) + \xi_4 \left(T_{AT}(t) - T_{LO}(t)\right), \end{aligned} \tag{10}$$

where ξ_i and η calibration parameters for an assumed climate sensitivity of 3°C that corresponds to the best estimate given by the IPCC (2013).

Increasing temperature triggers climate changes that yield economic losses affecting regional production (see again Eq. (3)). These (net) regional damages take into account the effects of adaptation (AD):

$$\mathrm{ELF}(j,t) = 1 - \mathrm{AD}(j,t)\left(\frac{T_{AT}(t) - T_d(j)}{cat_T(j) - T_d(j)}\right)^2, \tag{11}$$

where $T_d(j)$ is the temperature deviation (from pre-industrial level) at which damages start to occur in region $j = 1, \ldots, n$ and $cat_T(j)$ is the 'catastrophic' temperature level that dependends on the assumed climate sensitivity and at which the entire production of region j would be wiped out. To reduce the damaging effects of climate change, regions can invest in an adaptation stock. Adaptation dynamics in each region j is then modelled as follows:

$$\mathrm{AD}(j,t) = 1 - \alpha_{\mathrm{AD}}(j)\frac{K_3(j,t)}{K_{3\max}(j,t)}, \tag{12}$$

where α_{AD} is the maximal adaptation effectiveness and $K_{3\max}$ the maximal amount of adaptation capital that would ensure the optimal effectiveness of the adaptation measures. The latter is modelled as an increasing function of temperature level to capture the fact that adaptation costs should increase whenever temperature (and therefore damages) increases:

$$K_{3\max}(j,t) = \beta_{\mathrm{AD}}(j)\left(\frac{T_{AT}(t)}{T_d(j)}\right)^{\gamma_{\mathrm{AD}}(j)}, \tag{13}$$

where β_{AD} and γ_{AD} are calibration parameters.

3 A differential game with coupled constraint

3.1 A coupled isoperimetric constraint

We model the competition of different countries to tackle climate change as a differential game having the following structure. Eqs. (14)-(15) are the state equations and initial conditions for the decoupled variables and controls of the players $j = 1\dots,m$; in our case they are the capital stocks and the investment, labor allocation and emission variables. Eq. (16) corresponds to the decoupled state and control constraints for each of the players j. Eqs. (17)-(18) are the state equations and initial conditions for the coupling state variable, in our case they are the climate state variables:

$$
\begin{aligned}
\dot{x}_j(t) &= f_j(t, x_j(t), u_j(t)), \quad j = 1\dots,m && (14)\\
x_j(0) &= x_j^o, \quad j = 1\dots,m && (15)\\
0 &\geq h_j(t, u_j(t), x_j(t)), \quad j = 1\dots,m && (16)\\
\dot{y}(t) &= g(t, \bar{x}(t), y(t), u(t)) && (17)\\
y(0) &= y^o. && (18)
\end{aligned}
$$

The payoff to player j is given by the integral:

$$\int_0^\infty e^{-\rho t} L_j(t, x_j(t), u_j(t), y(t))\, dt, \quad j = 1\dots,m. \tag{19}$$

These variables and functions have the following dimensions:

$$x_j \in \mathbb{R}^{n_j}, u_j \in \mathbb{R}^{p_j},\ j = 1\dots,m, \quad y \in \mathbb{R}^q.$$

$$f_j : \mathbb{R} \times \mathbb{R}^{n_j} \times \mathbb{R}^{p_j}, \to \mathbb{R}^{n_j}, \quad h_j : \mathbb{R} \times \mathbb{R}^{n_j} \times \mathbb{R}^{p_j}, \to \mathbb{R}^{\nu_j},\ j = 1\dots,m.$$

$$g : \mathbb{R} \times \mathbb{R}^n \times \mathbb{R}^q, \to \mathbb{R}^q, \quad n = \sum_j n_j, \quad L_j : \mathbb{R} \times \mathbb{R}^{n_j} \times \mathbb{R}^{p_j} \times \mathbb{R}^q \to \mathbb{R}.$$

The climate agreement is summarized by the definition of a global budget (BUD) for the sum of emissions from all players defined by the functions $\sum_j \ell_j(u_j(t))$, $\ell_j : \mathbb{R}^{p_j} \to \mathbb{R}$, over a planning period $[t_0, t_1]$. This is written:

$$\int_{t_0}^{t_1} \sum_j \ell_j(u_j(t))\, dt \leq \text{BUD}, \tag{20}$$

where $\ell_j : \mathbb{R}^{n_j} \to \mathbb{R}$. This is a coupled constraint imposed on the differential game. We will show that finding a normalized equilibrium for the game with coupled constraints is equivalent to computing a Nash equilibrium with the following decoupled constraints:

$$\int_{t_0}^{t_1} \ell_j(u_j(t))\, dt \leq \theta_j \text{BUD} \quad \text{j} = 1\dots,\text{m}, \tag{21}$$

with:

$$0 \leq \theta_j, \;\; j = 1 \ldots, m, \quad \sum_j \theta_j = 1. \tag{22}$$

Varying the shares θ_j of the global emission budget going to each player $j = 1 \ldots, m$, one generates the whole manifold of normalized equilibria. So a second part of the agreement will be the choice of a particular set of θ_j's under some fairness criteria.

3.2 The manifold of normalized equilibria

Given the initial state, the payoff functions of each player can be written $\phi_j(\underline{u}_{M-j}(\cdot), u_j(\cdot))$, where $\underline{u}_{M-j}(\cdot)$ denote the controls of the players other than j and $u_j(\cdot)$ is the control of player j, over the whole time interval $[0, \infty)$. The coupled constraint is denoted $\underline{u}(\cdot) \in \mathcal{U}$. Let $\mathbf{r}$ be a vector of positive weights $r_j > 0$, $\underline{u}(\cdot)$ and $\underline{v}(\cdot)$ two m control vectors. We define the response function with weighting $\mathbf{r}$ as:

$$\Psi(\underline{u}(\cdot), \underline{v}(\cdot); \mathbf{r}) = \sum_j r_j \, \phi_j(\underline{u}_{M-j}(\cdot), v_j(\cdot)) \tag{23}$$

and the optimal response map as the set valued mapping:

$$\Upsilon(\underline{u}(\cdot); \mathbf{r}) = \left\{ \underline{v}^o(\cdot) = \mathrm{argmax}_{\underline{v}(\cdot) \in \mathcal{U}} \, \Psi(\underline{u}(\cdot), \underline{v}(\cdot); \mathbf{r}) \right\}. \tag{24}$$

An m-control vector $\underline{u}^\star(\cdot)$ is an equilibrium under the coupled constraint $\underline{u}(\cdot) \in \mathcal{U}$, if it is a fixed point of the optimal response mapping, i.e, if the following holds:

$$\underline{u}^\star(\cdot) \in \Upsilon(\underline{u}^\star(\cdot); \mathbf{r}). \tag{25}$$

In our particular case the constraint set $\mathcal{U}$ is defined by the inequality:

$$\int_{t_0}^{t_1} \sum_j \ell_j(u_j(t)) \, dt - \mathrm{BUD} \leq 0 \tag{26}$$

Assuming enough regularity, the optimization in (24) implies the existence of a multiplier μ verifying:

$$0 = \mu \left(\int_{t_0}^{t_1} \sum_j \ell_j(u_j(t)) \, dt - \mathrm{BUD} \right) \tag{27}$$

$$0 \leq \mu. \tag{28}$$

Then the necessary optimality conditions at equilibrium are the same as those for a Nash equilibrium in the differential game with modified payoffs given by:

$$\begin{aligned} J_j &= \int_0^{t_0} e^{-\rho t} L_j(t, x_j(t), u_j(t), y(t))\, dt \\ &+ \int_{t_0}^{t_1} e^{-\rho t} \left(L_j(t, x_j(t), u_j(t), y(t))\, dt - \frac{\mu}{r_j} \sum_{i=1}^{m} \ell_i(u_i(t)) \right) dt \\ &+ \int_{t_1}^{\infty} e^{-\rho t} L_j(t, x_j(t), u_j(t), y(t))\, dt \quad j = 1 \ldots, m. \end{aligned} \tag{29}$$

Now it is easy to verify that these optimality conditions are equivalent to those of a Nash equilibrium with decoupled constraints:

$$\int_{t_0}^{t_1} \ell_j(u_j(t))\, dt - \theta_j \mathrm{BUD} \quad \mathrm{j = 1 \ldots, m.} \tag{30}$$

Indeed, at a Nash equilibrium there will exist multipliers μ_j satisfying:

$$0 = \mu_j \left(\int_{t_0}^{t_1} \ell_j(u_j(t))\, dt \leq \theta_j \mathrm{BUD} \right). \tag{31}$$

$$0 \leq \mu_j, \quad j = 1, \ldots, m. \tag{32}$$

Since the constraint is scalar (one dimensional) so is also each μ_j. If we define $\mu = \sum_j \mu_j$ and $r_j = \frac{\mu}{\mu_j}$ we can write these optimality conditions as in Eqs. (27)-(28). Therefore there is a one-to-one correspondence between the manifold of normalized equilibria, indexed over the weighting $\mathbf{r}$ and the set of Nash equilibria with decoupled constraints (30), indexed over the possible sharings of the global budget defined by

$$\begin{aligned} 0 &\leq \theta_j, \quad j = 1 \ldots, m \\ 1 &= \sum_j \theta_j. \end{aligned} \tag{33}$$

3.3 Economic interpretation

The introduction of a coupled constraint in the equilibrium game, based on a global emission budget over a given commitment period, can be interpreted as equivalent to the introduction of a tax on emissions. In the model emissions are represented by the function $\ell_j(u_j)$[1] during the period $[t_0, t_1]$,

[1]In the model we use $\ell_j(u_j)$ is the projection of the control vector on the emission component.

and depending on the weighting $\mathbf{r}$ the tax $\frac{\mu}{r_j}$ is different in each group of countries. We notice that the tax is increasing in current value, since the direct sum of emissions is considered and not their discounted sum. This has the interesting effect of preventing a large increase of emissions at the end of the $[t_0, t_1]$ period.

4 Numerical illustration

In this section we solve numerically a differential game having the structure described in Section 3 and where the players dynamics correspond to the integrated economic growth model of Section 2. There are three players, corresponding roughly to industrialized (OECD), emerging (BRIC) and developing or rest of the world (ROW) countries. Each player j controls a decoupled economic system through the accumulation of three sorts of capital ($K_i(j,t)$, $i = 1, \ldots, 3$) and has an influence, through the accumulation of its GHG emissions, on the climate dynamics. The temperature increase causes a loss of economic output in each economy and this creates an interdependence between the players that leads to the formulation of the fundamental game structure of the climate change issue.

Assuming that each player develops its economic systems in order to optimize the discounted sum of utility derived from consumption, over an infinite time horizon, we will first compute the solution of the Pareto and Nash equilibrium solutions of the open-loop differential game, and compare them with the BAU case, obtained when we assume that there is no economic damage caused by temperature increase. Notice that, in this case, the players control totally decoupled systems and the game situation disappears.

In a second part, we introduce a constraint in the Pareto solution, which consists in keeping the temperature increase below 2°C, forever, as proposed in the Copenhagen Accord (United Nations, 2009). We use the emission budget over the period 2010-2050 or 2010-2070 obtained in this Pareto solution to introduce a coupled constraint in the non-cooperative game. We next compute the normalized equilibrium corresponding to a sharing of the budget that is the same as in the Pareto solution. We compare then the normalized equilibrium solution with the simple Nash equilibrium obtained earlier

Finally, in a third part, we explore the effect of modifying the shares of the global emission budget on a fairness criterion designed around the discounted sum of consumption of the population concerned during the commitment period.

All the calculations are made using a simple discretization of the dynamics, leading to difference equations. A mathematical programming approach is then used to solve the optimization problems, using GAMS with CONOPT. The equilibrium solutions are obtained by solving a fixed point problem via a cobbweb approach[2]. Please also refer to the Appendices at the end of the manuscript.

4.1 Cooperative vs. non-cooperative solutions

In this section we first compare the results obtained in the baseline (denoted BAU), Pareto and Nash equilibrium solutions.

4.1.1 GHG emissions and temperature

In Table 1, we show first temperature deviation paths from preindustrial levels. In the BAU scenario, temperature reaches around 3.6°C by 2100. This

Table 1: Temperature deviation paths (in °C)

	BAU	Pareto	Nash
2010	0.9	0.9	0.9
2020	1.2	1.1	1.2
2030	1.4	1.4	1.4
2040	1.7	1.6	1.7
2050	2.0	1.8	1.9
2060	2.3	2.1	2.2
2070	2.6	2.2	2.5
2080	2.9	2.4	2.8
2090	3.3	2.6	3.1
2100	3.6	2.7	3.4

corresponds approximately to the *Representative Concentration Pathways* RCP8.5 scenario of the IPCC (2013) where the mean concentration reaches 3.7°C by 2100. When taking into account climate damages, and assuming that the three regions are collaborating to reach a Pareto equilibrium[3], temperature reaches a much lower level (2.7°C by 2100), but still above the safe limit of 2°C set by the Copenhagen Accord. In the Nash equilibrium setting, as each player optimizes its own welfare without consideration of the other

[2]Even though it is well known that cobweb does not always converge, we never had such an occurrence in our numerical experiments.

[3]By optimizing a weighted sum of their social welfare, with each weight set to 1/3.

players' welfare, the environmental situation deteriorates with temperature reaching 3.4°C by 2100, close to the BAU level. Table 2 shows next GHG emission levels for the three players.

Table 2: Emission paths (in GtC)

	BAU			Pareto			Nash		
	1	2	3	1	2	3	1	2	3
2010	1.9	3.5	3.2	1.5	3.1	2.9	1.8	3.3	3.1
2020	2.0	4.3	4.1	1.6	3.7	3.5	1.9	4.0	3.8
2030	2.2	5.1	4.9	1.8	4.3	4.1	2.1	4.7	4.5
2040	2.4	6.0	5.8	1.9	4.9	4.7	2.3	5.5	5.3
2050	2.8	7.0	6.8	2.1	5.5	5.3	2.6	6.3	6.1
2060	3.2	8.2	7.9	1.6	4.1	3.9	2.9	7.1	6.9
2070	3.6	9.4	9.0	1.5	3.8	3.7	3.3	8.0	7.8
2080	4.1	10.7	10.4	1.5	4.0	3.8	3.7	9.0	8.7
2090	4.7	12.2	11.8	1.6	4.2	4.1	4.2	10.0	9.7
2100	5.3	13.8	13.3	1.8	4.6	4.4	4.7	11.0	10.7

In the Pareto scenario, the reduction effort is until 2050 more important for Player 1 (OECD countries) than for the other two players. But after 2050, all players have about the same reduction effort (in % from the baseline). By contrast, in the Nash equilibrium scenario, where each player acts selfishly, they all emit more than in the Pareto scenario, especially Player 1.

4.1.2 Capital accumulation paths

Low-carbon capital accumulation levels are given in Table 3.

Table 3: Low-carbon capital K_2 accumulation paths (in trillion USD)

	BAU			Pareto			Nash		
	1	2	3	1	2	3	1	2	3
2010	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
2020	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
2030	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
2040	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
2050	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
2060	0.0	0.0	0.0	24.5	62.3	60.0	0.0	0.0	0.0
2070	0.0	0.0	0.0	37.0	95.0	91.5	0.0	0.0	0.0
2080	0.0	0.0	0.0	45.6	118.0	113.7	0.0	0.0	0.0
2090	0.0	0.0	0.0	53.2	138.2	133.3	0.0	0.0	0.0
2100	0.0	0.0	0.0	60.6	158.3	152.7	0.0	0.0	0.0

The accumulation of low-carbon capital K_2 and thus the use of clean energy sources are directly related to the emission reduction efforts carried out by the players. Neither in the baseline, where there is no climate change related damages, nor in the Nash case, where each player is more concerned about his own (rather short-term term[4]) welfare, does low-carbon capital accumulate. By contract, in the Pareto scenario, all regions start accumulating low-carbon capital by 2060, at a time when they more significantly curb their GHG emissions (compared to baseline levels). Table 4 shows the accumulation path of carbon-intensive capital K_1. Both in the base-

Table 4: Carbon-intensive capital K_1 accumulation paths (in trillion USD)

	BAU			Pareto			Nash		
	1	2	3	1	2	3	1	2	3
2010	47.3	41.5	36.4	47.1	41.4	36.2	47.3	41.5	36.3
2020	45.4	66.1	60.7	45.0	65.8	60.4	45.3	66.0	60.6
2030	48.6	92.9	87.4	48.0	92.3	86.8	48.5	92.8	87.3
2040	54.9	121.6	115.7	54.2	119.9	114.1	54.8	120.6	114.8
2050	63.7	152.2	145.8	62.7	150.0	143.7	63.3	150.8	144.5
2060	74.3	185.2	178.0	48.7	120.3	115.5	73.8	183.1	176.0
2070	86.7	220.9	212.7	47.8	120.9	116.4	86.0	217.7	209.7
2080	100.6	259.5	250.1	52.2	133.2	128.4	100.1	254.7	245.6
2090	116.0	301.2	290.5	56.9	150.6	145.3	112.6	294.2	283.8
2100	132.8	346.2	333.9	65.0	170.8	164.8	129.2	336.1	324.4

[4]As reflected by the pure time preference discount rate ρ in Eq (1).

line and in the Nash scenarios, the stock of carbon-intensive capital keeps increasing, as there is in these settings a lack of (serious) effort to abate GHG emissions. Conversely, in the Pareto scenario, carbon-intensive capital accumulates steadily only until one starts to invest in low-carbon capital. Afterwards, the carbon economy co-exists with the low-carbon one, but at reduced levels (compared to the baseline).

Table 5 reports finally on the accumulation of adaptation capital K_3. Note first that adaptation capital does not accumulate in the baseline, where

Table 5: Adaptation capital K_3 accumulation paths (in trillion USD)

	BAU			Pareto			Nash		
	1	2	3	1	2	3	1	2	3
2010	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
2020	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
2030	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
2040	0.0	0.0	0.0	0.0	1.1	1.1	0.0	1.1	1.1
2050	0.0	0.0	0.0	0.0	1.4	1.4	0.0	1.5	1.5
2060	0.0	0.0	0.0	0.0	1.8	1.8	0.0	2.0	2.0
2070	0.0	0.0	0.0	0.0	2.1	2.1	0.0	2.6	2.6
2080	0.0	0.0	0.0	0.0	2.4	2.4	0.0	3.2	3.2
2090	0.0	0.0	0.0	2.7	2.7	2.7	4.0	4.0	4.0
2100	0.0	0.0	0.0	3.0	3.0	3.0	4.8	4.8	4.8

it is not needed. By contrast, adaptation capital starts accumulating in the Pareto and Nash scenarios, as early as 2040 for Player 2 and 3, but only toward the end of the century for Player 1. For the latter player, adaptation acts as a complement to the mitigation efforts started earlier (especially in the Pareto setting). For the former players, there is during some initial periods (especially in the Pareto setting) a clear substitution between adaptation and mitigation efforts. These differences highlight the different trade-off between costs of adaptation and reduction of (some of) climate damages for the players. Note also that in the Nash scenario, the required amount of adaptation capital for a maximal effectiveness is higher (compared to the Pareto scenario), as temperature reaches higher levels.

4.2 Equilibria with coupled constraints

This section explores the results obtained when imposing a coupled constraint limiting to 2°C the temperature increase. We call 'ParetoLT' the scenario corresponding to a Pareto solution under this constraint. When imposing this coupled constraint as a global emission budget over the period 2010-2050 we call 'Rosen5P' the normalized equilibrium solution. When the constraint is imposed over the 2010-2070 period, we call 'Rosen7P' the normalized equilibrium solution.

4.2.1 GHG emissions and temperature

Table 6 reports first on temperature deviation paths from preindustrial levels. In the ParetoLT scenario, temperature reaches the limit by the end of

Table 6: Temperature deviation paths (in °C)

	ParetoLT	Rosen5P	Rosen7P
2010	0.9	0.9	0.9
2020	1.1	1.1	1.1
2030	1.3	1.3	1.3
2040	1.5	1.5	1.5
2050	1.6	1.6	1.6
2060	1.7	1.8	1.7
2070	1.8	2.0	1.8
2080	1.9	2.3	2.0
2090	1.9	2.7	2.2
2100	2.0	3.0	2.6

the century (and remains at this level afterwards). Under a non-cooperative setting, temperature is kept in check only during the commitment period, where it follows the same path as in the cooperative setting. Afterwards, temperature quickly exceeds the 2°C temperature limit, as players return to a purely selfish (Nash) behavior. Table 7 reports on GHG emission levels for the three players. In the ParetoLT scenario, as in the unconstrained Pareto case, the reduction effort is initially more important for Player 1 than for the other two players. But here, to avoid temperature exceeding the 2°C limit, the other players join with similar effort (in % from the basline) as early as 2030. In the Rosen setting, players make similar reduction efforts as for the ParetoLT scenario during the commitment period. Afterwards, players return to their Nash emission pattern and emit much more GHGs, but especially (again) Player 1.

4.2.2 Capital accumulation paths

Low-carbon capital accumulation levels are given in Table 8. In the Pare-

Table 7: Emission paths (in Gt C)

	ParetoLT			Rosen5P			Rosen7P		
	1	2	3	1	2	3	1	2	3
2010	1.4	3.0	2.8	1.5	3.1	2.9	1.5	3.1	2.9
2020	1.0	3.4	3.3	1.3	3.6	3.4	1.3	3.6	3.4
2030	0.9	2.4	2.3	1.0	2.5	2.4	1.0	2.5	2.4
2040	0.8	2.2	2.1	0.9	2.2	2.2	0.9	2.2	2.1
2050	0.8	2.1	2.1	0.8	2.1	2.1	0.8	2.1	2.1
2060	0.8	2.0	2.0	2.5	6.2	6.0	0.7	2.0	1.9
2070	0.7	1.9	1.8	3.2	7.7	7.5	0.7	1.8	1.8
2080	0.6	1.6	1.6	3.7	8.9	8.7	3.2	7.7	7.5
2090	0.5	1.4	1.3	4.2	10.0	9.7	4.0	9.6	9.4
2100	0.4	1.1	1.1	4.7	11.1	10.8	4.7	11.0	10.7

Table 8: Low-carbon capital K_2 accumulation paths (in trillion USD)

	ParetoLT			Rosen5P			Rosen7P		
	1	2	3	1	2	3	1	2	3
2010	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
2020	13.4	0.0	0.0	7.8	0.0	0.0	7.4	0.0	0.0
2030	20.0	33.4	31.7	18.0	33.5	31.8	17.9	33.4	31.8
2040	24.7	53.9	51.5	24.1	54.0	51.6	24.0	54.0	51.6
2050	29.3	70.3	67.5	29.1	70.4	67.6	29.1	70.4	67.5
2060	34.3	85.8	82.5	10.2	24.6	23.6	34.2	85.8	82.6
2070	39.6	101.4	97.6	3.5	8.6	8.2	39.6	101.4	97.7
2080	45.4	117.4	113.2	1.2	3.0	2.9	13.8	35.4	34.1
2090	51.5	133.9	129.1	0.4	1.0	1.0	4.8	12.3	11.9
2100	57.8	150.7	145.4	0.2	0.4	0.3	1.7	4.3	4.1

toLT case, low-carbon capital K_2 accumulates throughout the century, as more clean energy sources are used. These accumulations are directly related to the emission reduction efforts carried out by the players. By contrast, in the Rosen setting, low-carbon capital only accumulates during the commitment period, when players make a substantial effort to abate emissions. Afterwards, low-carbon capital is phased out, as players are basically no longer concerned with emission control for the common good.

Table 9 gives next accumulation levels of carbon-intensive capital K_1. The development of the carbon economy is again (inversely) proportional

Table 9: Carbon-intensive capital K_1 accumulation paths (in trillion USD)

	ParetoLT			Rosen5P			Rosen7P		
	1	2	3	1	2	3	1	2	3
2010	47.1	41.3	36.2	47.2	41.4	36.2	47.2	41.4	36.2
2020	31.6	65.6	60.3	37.2	65.8	60.4	37.6	65.8	60.4
2030	27.8	58.8	55.0	29.9	59.0	55.2	30.0	59.0	55.1
2040	28.6	64.6	61.3	29.5	64.9	61.6	29.4	64.7	61.4
2050	31.5	75.7	72.4	32.2	76.7	73.6	31.8	75.8	72.6
2060	35.4	88.5	85.0	61.7	154.4	148.7	35.6	88.8	85.4
2070	39.7	101.6	97.8	81.2	206.6	199.1	40.7	103.8	100.2
2080	44.3	114.4	110.3	98.3	250.8	241.9	80.9	207.9	200.7
2090	48.6	126.4	121.8	113.0	293.8	283.5	106.0	275.8	266.2
2100	51.7	136.9	132.0	130.1	337.7	325.9	127.3	330.5	319.0

to the rise of the low-carbon economy and emission reduction efforts. More precisely, the carbon economy only flourishes in the Rosen setting when the commitment period is over. Otherwise, the carbon economy co-exists with the low-carbon one, but at reduced levels (compared to the baseline).

Table 10 reports finally on the accumulation of adaptation capital K_3. In the ParetoLT scenario, adaptation acts as a complement to the mitigation efforts started earlier by all players. The same happens in the coupled equilibrium (Rosen) setting during the commitment period. But here, when the commitment period is over, adaptation acts more and more as a substitute to the mitigation efforts with the progressive phase out of the low-carbon capital. Note also that when the commitment period is over, the required amount of adaptation capital for a maximal effectiveness is higher (compared to the ParetoLT scenario), as temperature reaches again higher levels.

Table 10: Adaptation capital K_3 accumulation paths (in trillion USD)

	ParetoLT			Rosen5P			Rosen7P		
	1	2	3	1	2	3	1	2	3
2010	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
2020	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
2030	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
2040	0.0	0.9	0.9	0.0	0.9	0.9	0.0	0.9	0.9
2050	0.0	1.0	1.0	0.0	1.1	1.1	0.0	1.1	1.1
2060	0.0	1.2	1.2	0.0	1.3	1.3	0.0	1.2	1.2
2070	0.0	1.3	1.3	0.0	1.7	1.7	0.0	1.4	1.4
2080	0.0	1.4	1.4	0.0	2.3	2.3	0.0	1.6	1.6
2090	0.3	1.5	1.5	3.0	3.0	3.0	2.1	2.1	2.1
2100	1.6	1.6	1.6	3.8	3.8	3.8	2.8	2.8	2.8

4.3 Consumption losses in the different games

Tables 11 and 12 report first on the relative variations (losses) of the discounted sum of consumption with respect to the BAU scenario for different (commitment) periods.

Table 11: Consumption losses over the period 2010-2050

	1	2	3
Pareto	1.08%	1.07%	1.07%
ParetoLT	1.41%	1.27%	1.27%
Nash	0.95%	1.00%	1.01%
Rosen5P	1.53%	1.44%	1.46%

These relative losses turn out to be quite close to each other in the different scenarios corresponding to different solution concepts. They range from 0.95% to 1.53% for the shorter commitment period considered, and from 1.38% to 2.15% for the longer one. In these two cases, the games with a coupled constraint on temperature (ParetoLT scenario) or on total GHG emissions during the commitment period (Rosen scenarios) yield the highest loses, as players invest heavily in low-carbon technology development to limit temperature increase or to respect a corresponding limit on global emissions. Conversely, in the Nash setting, losses are the lowest, as players do not make efforts to limit temperature increase during the periods considered, to their detriment in the long run.

Table 12: Consumption losses over the period 2010-2070

	1	2	3
Pareto	1.65%	1.51%	1.52%
ParetoLT	1.91%	1.74%	1.74%
Nash	1.48%	1.38%	1.39%
Rosen7P	2.15%	2.00%	2.01%

These variations could be considered as a criterion of fairness among the groups of countries participating in the climate negotiations. For example, it appears that the first group, Player 1, consistently loses more than the two other players during the commitment periods. The way the overall 'carbon budget' is shared among players plays thus a key role on how losses affect them. To explore further this issue, we have computed Rosen solutions for different sharing θ_j. Sharing has again been obtained from the Pareto solution when considering a limit of 2°C on temperature increase (ParetoLT scenario). Let us first recall that the first sharing considered so far as been computed with equal weights assigned to the players. We have also computed weights on a per capita basis (proportionally to initial population levels), and on a 'grand-fathering' basis (proportionally to initial emission levels). This yields respectively a second and third sharing θ_j. Results, in terms of income losses, are given in Tables 13 and 14.

Table 13: Consumption losses over the period 2010-2050

	1	2	3
Rosen5P, sharing #1	1.53%	1.44%	1.46%
Rosen5P, sharing #2	1.80%	1.40%	1.42%
Rosen5P, sharing #3	1.30%	1.41%	1.73%

Table 14: Consumption losses over the period 2010-2070

	1	2	3
Rosen7P, sharing #1	2.15%	2.00%	2.01%
Rosen7P, sharing #2	2.65%	1.91%	1.95%
Rosen7P, sharing #3	1.85%	1.93%	2.37%

As expected, compared to the first sharing where losses appear relatively similar between players, the second (per capita) sharing favors Players 2 and 3 where population levels are higher than in Player 1. Conversely, the third (grand-fathering) sharing favors Players 1 and 2 where initial GHG emission levels are higher than in Player 3.

5 Conclusion

In this paper, we have represented the climate negotiations and the resulting agreement as the imposition of a coupled constraint in a dynamic economic growth game, with a climate module and economic loss factor induced by temperature change. The economic growth models have two particular features. The players, i.e. the group of countries involved in the negotiations, can invest in a carbon and in a low-carbon economy. They can also invest in an adaptation capital which tends to alleviate the impact of climate change on economic production. We have shown that the normalized equilibria obtained under the coupled constraint, which consists in the definition of a global emission budget for the negotiated commitment period that has to be satisfied collectively by all the players, correspond to standard Nash equilibria for a differential game with decoupled constraints, where each player receives a share of the global budget and has to comply with this limit.

Using a 3-player model, corresponding to the division of the world economy into industrialized (OECD), emerging (BRIC) and developing (ROW) countries, and calibrated as in Bahn *et al.* (2012), we have simulated different possible solutions to the resulting differential game. The following two remarks can be made based on the obtained results:

1. The impact of climate change on the economy is important in the very long term. This implies that, in a cost-benefit approach, very little is done in early commitment periods (e.g., 2010-2050), even in a Pareto optimal solution. In order to obtain a sensible drive toward the use of low-carbon technologies, one must adopt a cost-effectiveness approach and impose a 2°C constraint on temperature increase in the Pareto optimal solution. Otherwise, even in the long-term, investment in adaptation capital is the favored (climate) policy.

2. A negotiation and climate agreement, based on this 2°C maximum temperature increase objective, is represented by the introduction of a coupled constraint for the three players, consisting in limiting the total emission budget over a commitment period to the emissions that would

result from a Pareto optimal solution with the temperature constraint. We show that the normalized equilibrium solutions corresponding to a Nash equilibrium under a particular sharing of the global budget can yield to moderate losses in consumption over the commitment period.

Our numerical illustration is based on a rather simple economic model, with a limited number of players. But our approach can be extended to more encompassing models, that would include for instance trade effects, as in REMIND-R or in WITCH. This modeling, that has put a cost-effectiveness structure in the climate economic game, has nonetheless shown that differential game models including a coupled constraint can shed some light on the assessment of possible climate negotiation outcomes.

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Appendices

A Model calibration

The calibration of the 3-player Ada-BaHaMa model follows the approach detailed in Bahn (2010) for a 2-player model. It is done for the Pareto scenario.

In short, the different economic and climate parameters (Eq. (1) to (10)) are mostly from the DICE model (version 2007[5], thereafter referred to as DICE2007). Compared to the carbon economy, production in the low-carbon economy has higher energy costs but a better energy efficiency. As a result, the overall production of the 3-player Ada-BaHaMa reproduces the economic output of DICE2007.

In addition, some regional parameter values have been adapted in the spirit of the RICE model. In particular, the three players have different population levels and initial values for capital accumulation in the carbon economy:

$L(j,0)$: initial value for population level of player j, in millions of persons; $L(1,0) = 1043.9$; $L(2,0) = 2731.5$; $L(3,0) = 2635.5$;

$K_1(j,0)$: initial value for carbon intensive capital of player j, in trillions USD; $K_1(1,0) = 60.2$; $K_1(2,0) = 20.6$; $K_1(3,0) = 16.6$.

[5]Nordhaus, W. "Notes on how to run the DICE model". In Yale University. [On line]. http://nordhaus.econ.yale.edu/DICE2007.htm (Website accessed on October 13, 2010).

Damages and adaptation parameters (Eq. (11) to (13)) are from the AD-DICE model (de Bruin *et al.*, 2009) and the World Bank (Margulis & Narain, 2009). Note that the maximal adaptation effectiveness is assumed to be 0.33 in all three regions. As a result, Ada-BaHaMa reproduces the overall magnitude of climate change damages estimated by DICE2007 and AD-DICE.

B GAMS code

The different GAMS codes used to perform our numerical experiments are availlable from http://www.ordecsys.com. We provide in particular:

Ada_Bahama-3pBAU.gms: the code to run our baseline (BAU) scenario;

Ada_Bahama-3pPareto.gms: the code to run our Pareto scenario;

Ada_Bahama-3pNash.gms: the code to run our Nash scenario;

Ada_Bahama-3pRosen.gms: the code to run our Rosen scenarios.